

The ML Abstract Machine

The state of the Abstract Machine (AM) is determined by four quantities (together with their denotations):

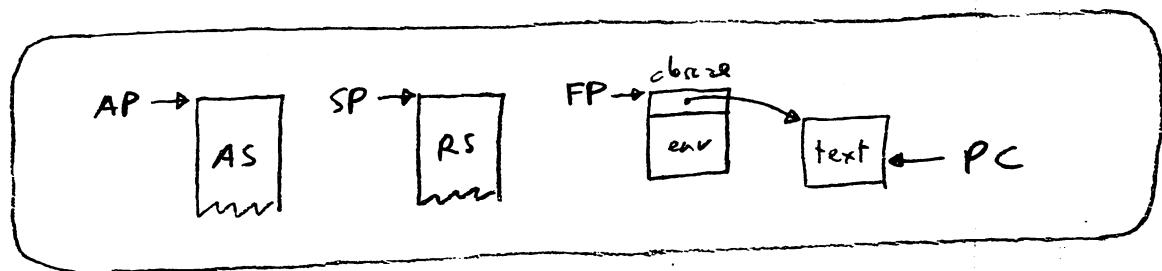
AP - Argument Pointer : Pointer to the top of the Argument Stack (AS), where arguments are loaded to be passed to functions, and results of functions are delivered. This stack is also used to store local and temporary values.

FP - Frame Pointer : Pointer to the current closure consisting of the text of the currently executed program, and of an environment for the free variables of the program.

SP - Stack Pointer : Pointer to the top of the Return Stack (RS), where program counter and frame pointer are saved during function calls.

PC - Program Counter : Pointer to the next instruction to be executed inside the current program.

Here is a snapshot of the AM:



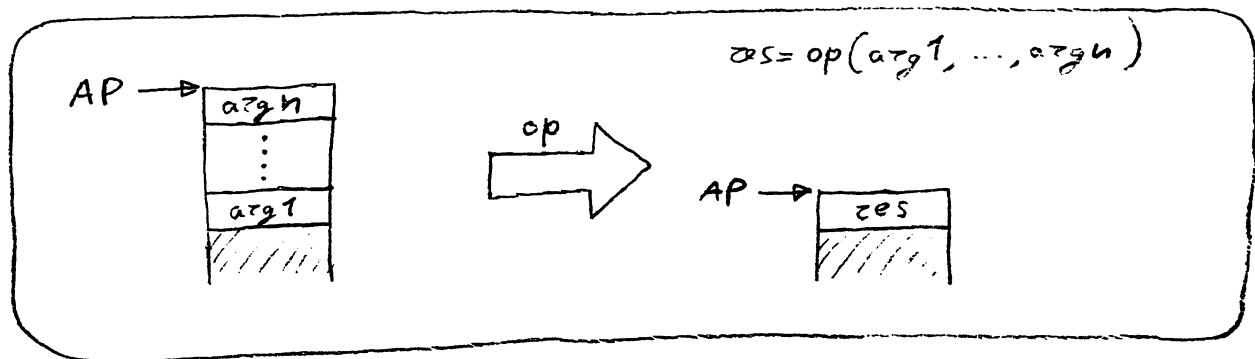
- The AM assumes the existence of an infinite memory of cells of different sizes -
Typical cells are null, bool, num, text, ref, pair, list,
injection, closure and text cells - The exact format
of these cells is immaterial, as long as the primitive
operations on these cells respect the expected properties.

The AM does not assume these cells to
contain any information about their type -

- Stacks, closures, texts and data contain pointers
to cells, and this convention will be strictly
observed in these notes. However implementations
may directly store certain cells, instead of their
pointers, on stacks etc; this usually happens for null,
empty, bool and num cells, but should never happen for
ref cells -

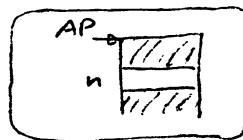
Data Operations

These are operations which transfer data back and forth between the Argument Stack and data cells - With the exception of destructors (see below) they take n arguments ($n \geq 0$) from the top of AS (the first argument is the deepest one) popping AS n times. Then they push their result back on the top of AS -



Note that the typechecking of the ML source program will guarantee against any misuse of AM operations -

The notation

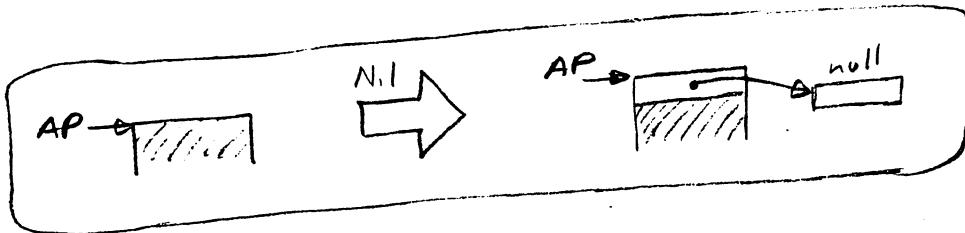


means that " n " is a

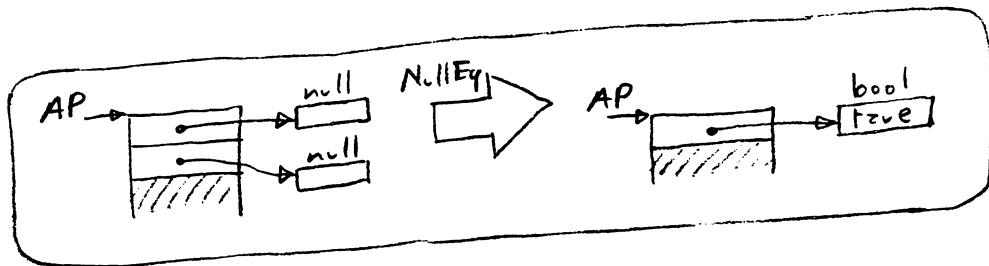
displacement from the top of AS where the top has displacement 0 -

Null Operations

• Nil



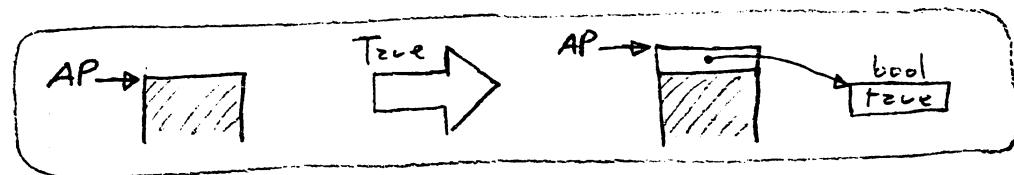
• NullEq



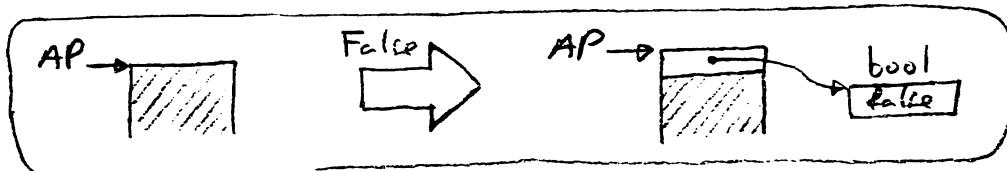
• NullPoint

Boolean Operations

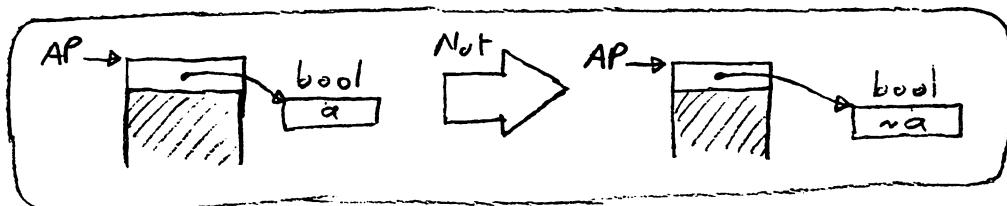
- True



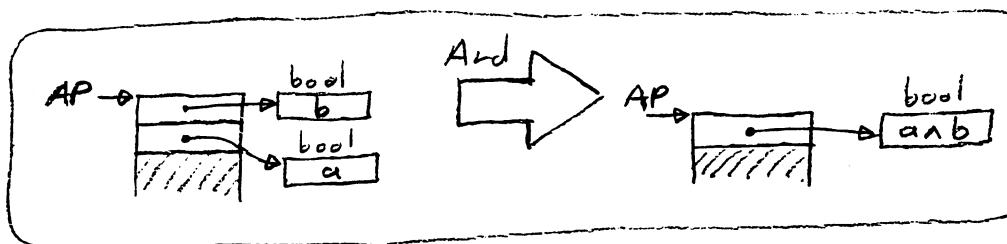
- False



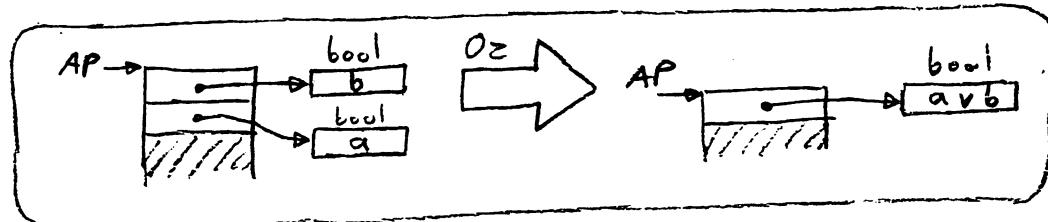
- Not



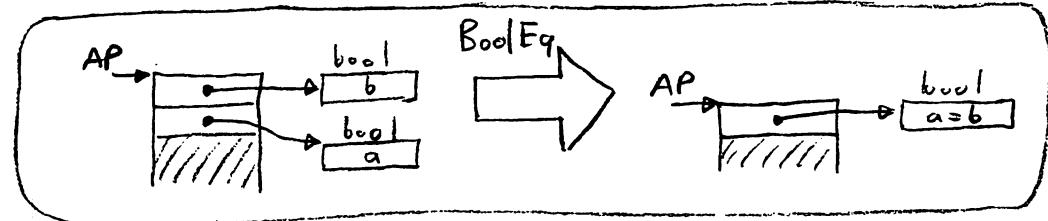
- And



- Or



- BoolEq



- Bool Point

Numeric Operations

All numbers are real numbers -

- Num n (*push a new cell containing n on AS*)
- Minus ($\text{Minus}(a) = -a$)
- Plus ($\text{Plus}(a, b) = a + b$)
- Diff ($\text{Diff}(a, b) = a - b$)
- Times ($\text{Times}(a, b) = a * b$)
- Divide ($\text{Divide}(a, b) = a / b$)
- IntDiv ($\text{IntDiv}(a, b) = \lfloor a / b \rfloor$)
- Module ($\text{Module}(a, b) = (a / b) - \lfloor a / b \rfloor$)
- Greater ($\text{Greater}(a, b) = a > b$)
- Less ($\text{Less}(a, b) = a < b$)
- GreatEq ($\text{GreatEq}(a, b) = a \geq b$)
- LessEq ($\text{LessEq}(a, b) = a \leq b$)
- NumEq ($\text{NumEq}(a, b) = a = b$)
- NumPnt

String Operations

- Tok `...' (push a cell containing `...' on AS)
- Conc ($\text{Conc}(`...', `---') = `...---`$)
- SubTok ($\text{SubTok}(k, l, `c_1 \dots c_n') = `c_k \dots c_{k+l-1}'$)
- TokLength ($\text{TokLength}(`c_1 \dots c_n') = n$)
- Explode ($\text{Explode}(`c_1 \dots c_n') = [`c_1'; \dots; `c_n']$)
- Implode ($\text{Implode}([`--_1'; \dots; `--_n']) = `..., \dots, --_n'$)
- Search ($\text{Search}(`f_0 \dots p_n', `...q_1 \dots q_m \dots') = n$
where $p_i = q_{n+i}$ (first occurrence from left)
fails if no occurrence)
- TokEq ($\text{TokEq}(`p_1 \dots p_n', `q_1 \dots q_m') = (n=m) \wedge (p_i = q_i \forall i)$)
- TokPrint
- TokUQPrint (print UnQuoted)

Reference Operations

- Fetch

$(\text{Fetch}(z) = a \text{ where } z = \text{ref}(a))$

- Store

$(\text{Store}(a, z) = (z := a; a))$

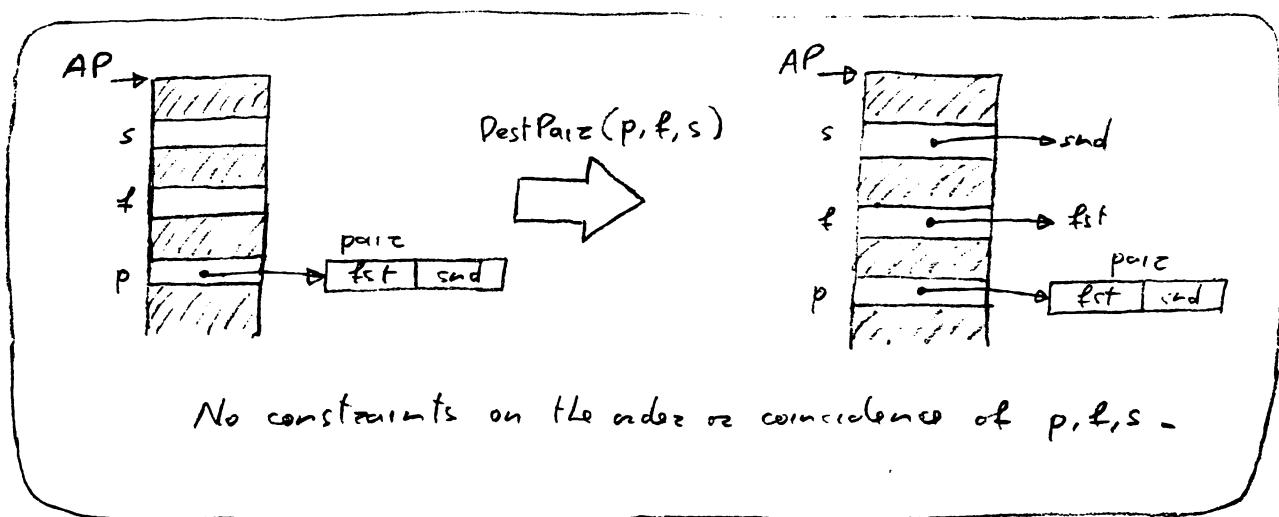
- RefEq

$(\text{RefEq}(z_1, z_2) = (a_1 = a_2) \text{ where } z_1 = \text{ref}(a_1); z_2 = \text{ref}(a_2))$

- RefPoint

Pair Operations

- **Pair** ($\text{Pair}(f, s)$ pushes a pair cell (f, s) on AS)
- **Fst** ($\text{Fst}(p) = f$ where $p = f, s$)
- **Snd** ($\text{Snd}(p) = s$ where $p = f, s$)
- **DestPair**

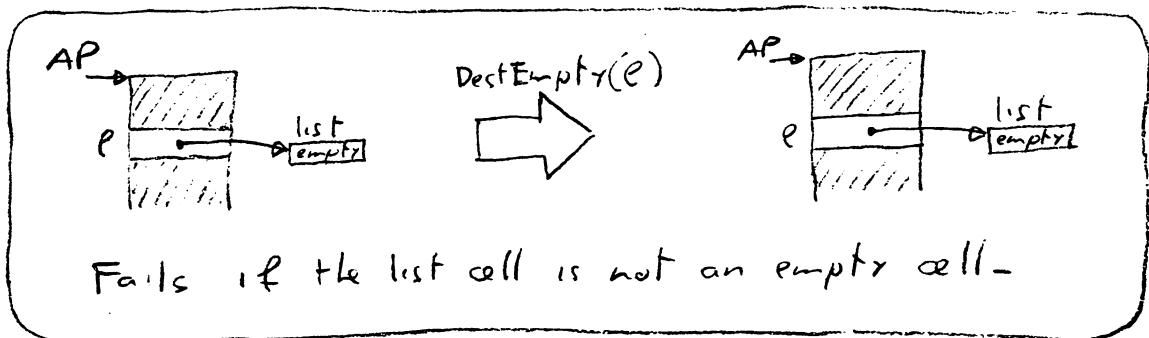


- **Pair Point**

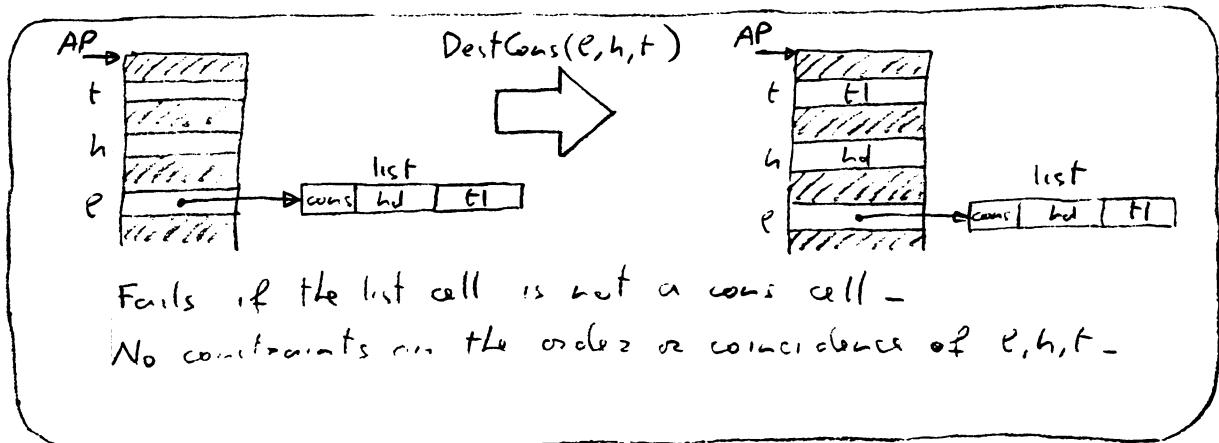
List Operations

- Empty (push a list empty cell on AS)
- Cons (Cons(h, t) pushes a list cons cell (h-t) on AS)
- Hd ($Hd(e) = h$ where $e = h-t$)
- Tl ($Tl(e) = t$ where $e = h-t$)
- Null ($Null(e) = e = []$)

• DestEmpty



• DestCons



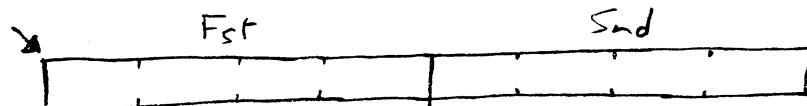
• Cons Point

Disjunction Operations

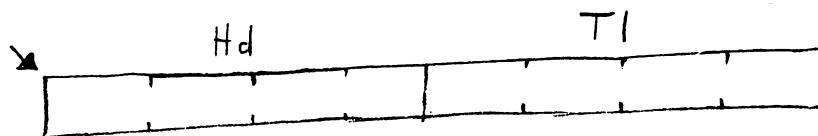
- Inl ($\text{Inl}(a)$ pushes a left injection cell (a) on AS)
- Inr ($\text{Inr}(a)$ pushes a right injection cell (a) on AS)
- Outl ($\text{Outl}(j) = a$ where $j = \text{inl}(a)$)
- Outr ($\text{Outr}(j) = a$ where $j = \text{inr}(a)$)
- Isl ($\text{Isl}(j) = (\exists a) j = \text{inl}(a)$ for some a)
- Isr ($\text{Isr}(j) = (\exists a) j = \text{inr}(a)$ for some a)
- DisjPoint

ML Run-Time Data Structures

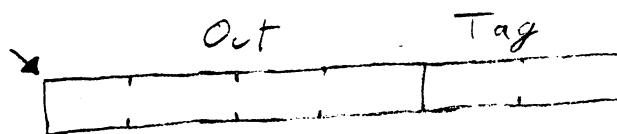
Pair



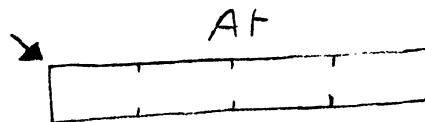
Cons



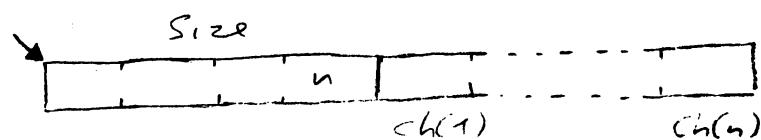
Injection



Reference



Token



Empty

0

True

1

False

0

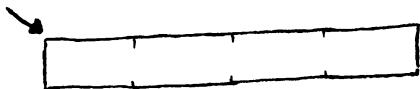
Nil

0

Integer

-32768 .. 32767

Number



(Contains a Floating Point)

Note: Empty, True, False, Nil and Integers are Unboxed values.

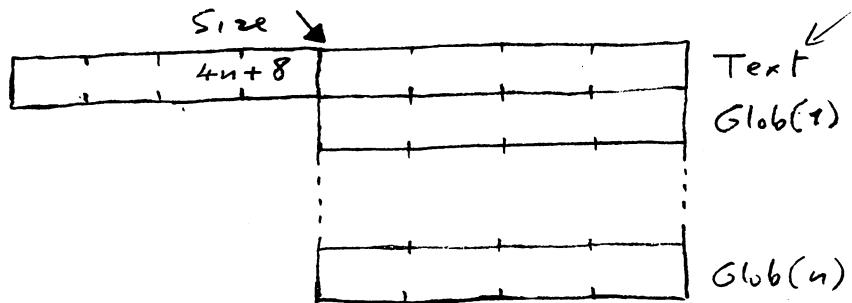
They are contained directly on the stack or inside data structures - When an unboxed value (occupying a word) is

contained in the least significant part of a long word
(e.g. in a pair) the other word must be zero -

Pointers can be distinguished from unboxed values

because the most significant word of a pointer cannot be zero -

Closure

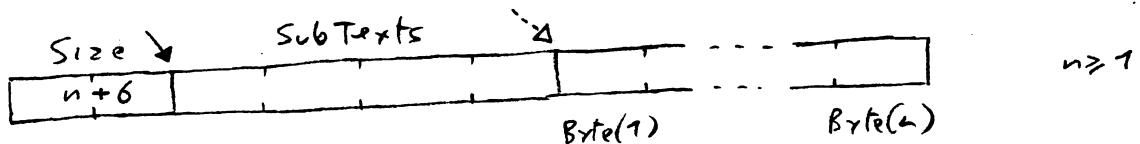


machine code. block.

$n \geq 0$

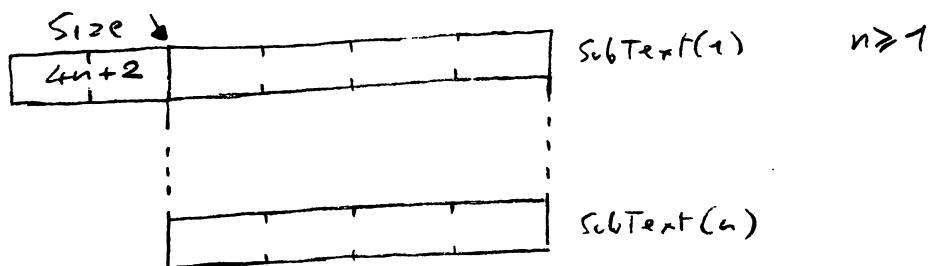
The **Size** field
is also used by
the Collector
to save +6 Text
pointer

Text⁽ⁿ⁾



$n \geq 1$

SubText



$n \geq 1$

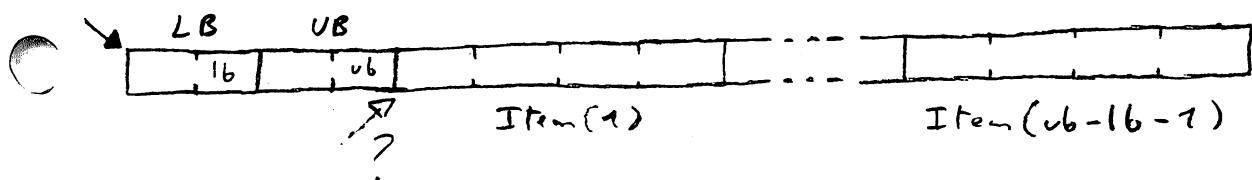
(1) The pointer \rightarrow is used when passing Texts around by themselves (it is convenient for garbage collection);

(2) The pointer $\rightarrow\rightarrow$ is used when referring to a Text from a closure (it is convenient for function application).

"Size" fields are placed before the arrows \rightarrow and $\rightarrow\rightarrow$ because they are only used during garbage collection.

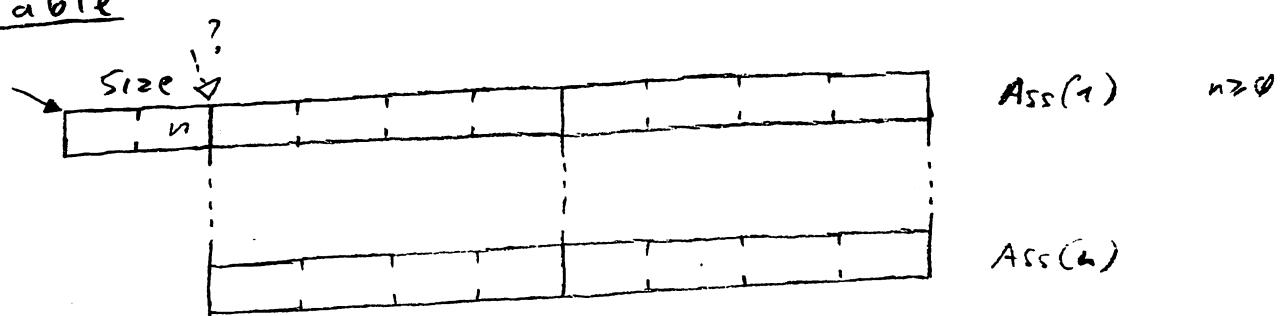
Array

$$ub+1 \geq lb$$



Table

$$Ass(1) \quad n \geq 0$$



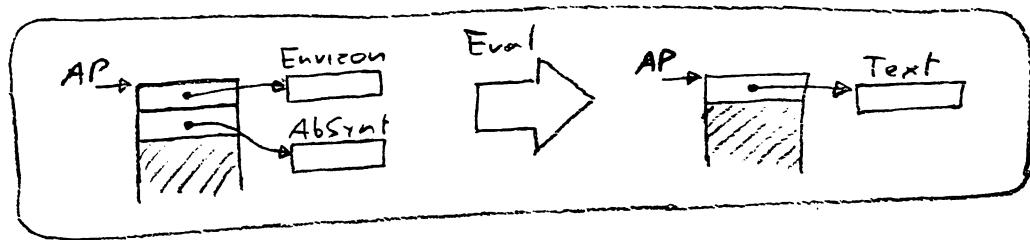
$$Ass(2)$$

Abstract Syntax Operations

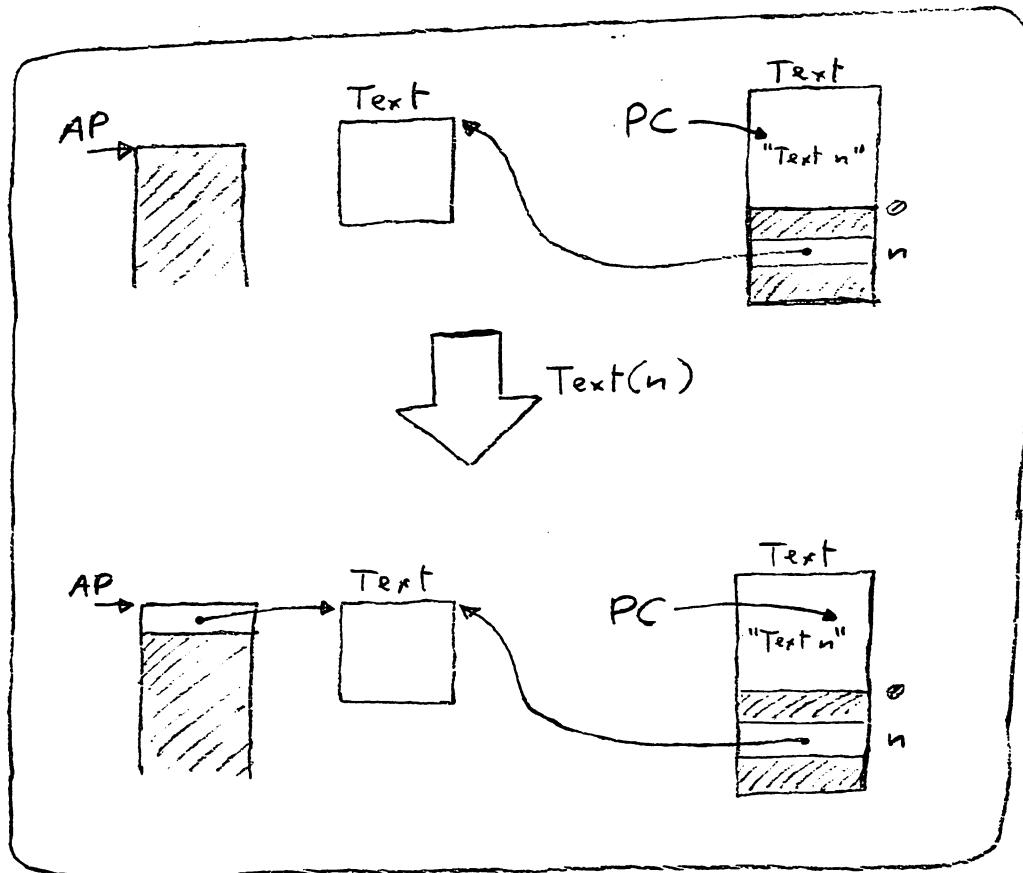
- Parse (read a string and push a parse tree on AS)
- - - -
 - { make-dec-*i*s primitives for each syntactic clause

Text Operations

- Eval

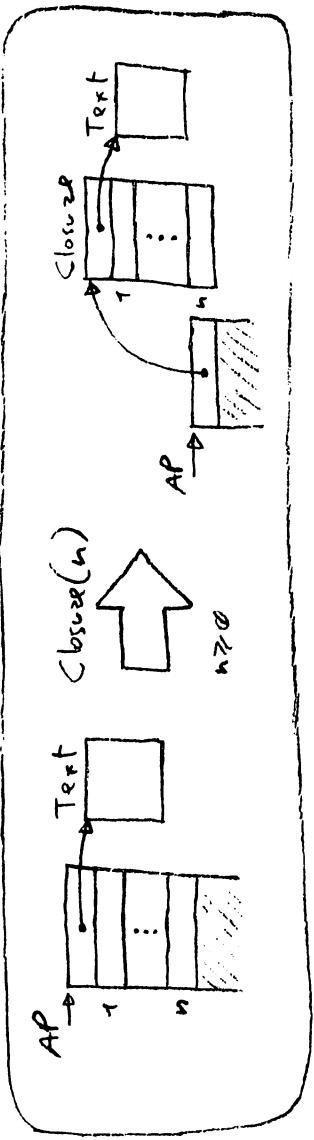


- Text

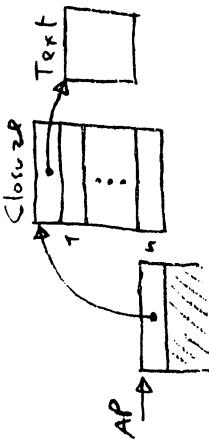


Closure Operations

C. Closure



Closure



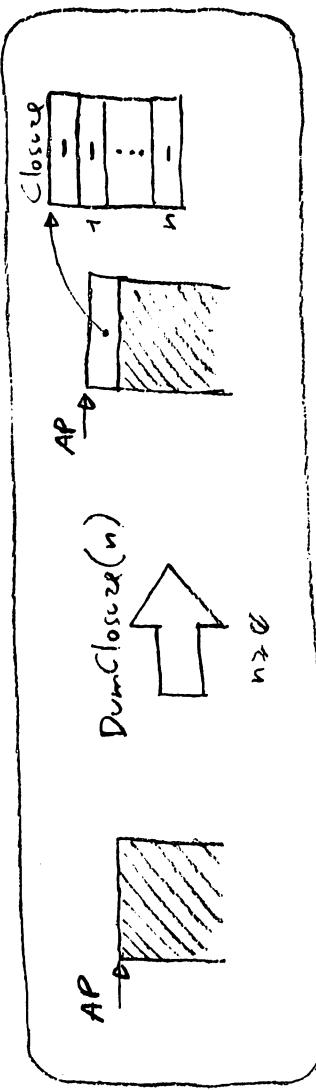
Closure

Closure(n)



$n \geq 0$

D. DerefClosure



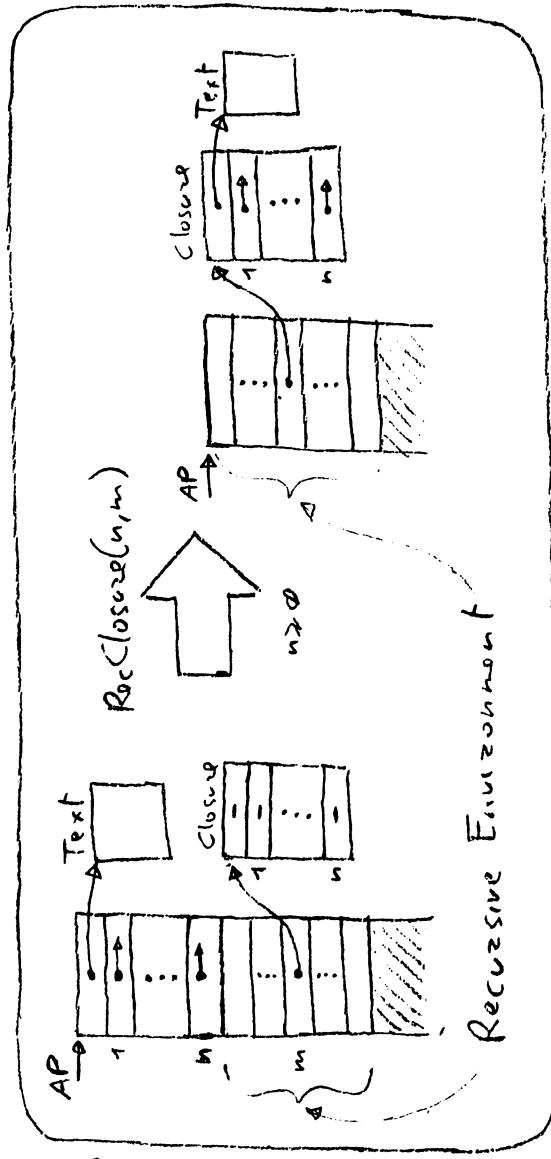
DerefClosure

(n)



$n \geq 0$

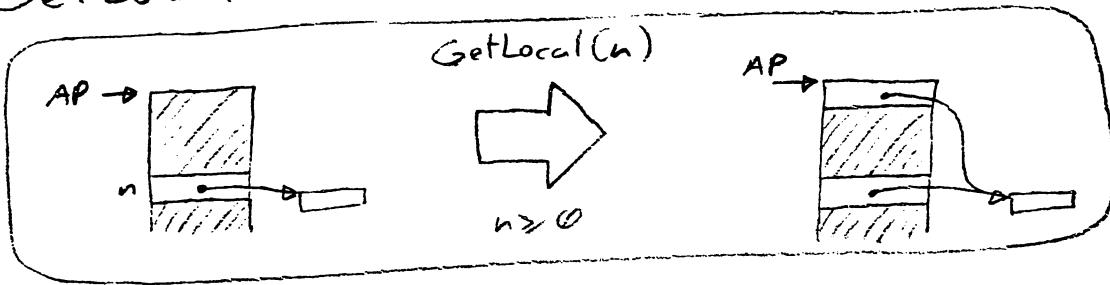
E. RecClosure



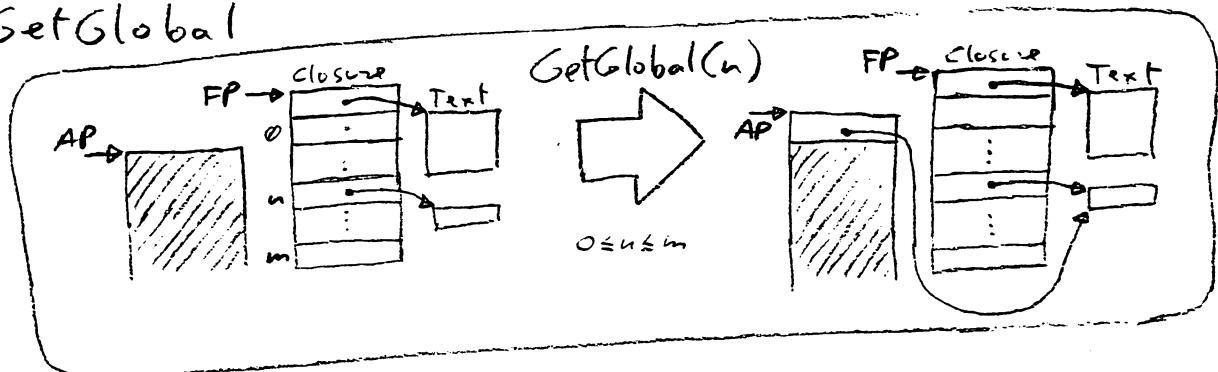
F. Closure Point

Stack Operations

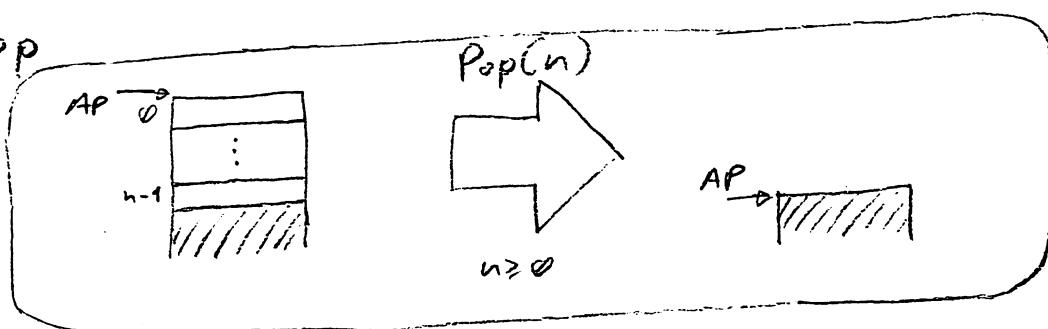
• GetLocal



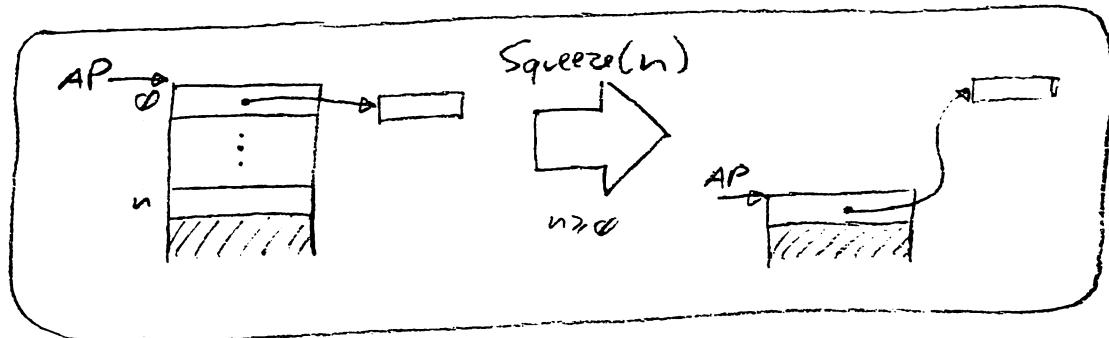
• GetGlobal



• Pop



• Squeeze



• Rise

Control Operations

- These are operations affecting the Program Counter and the Stack Pointer -

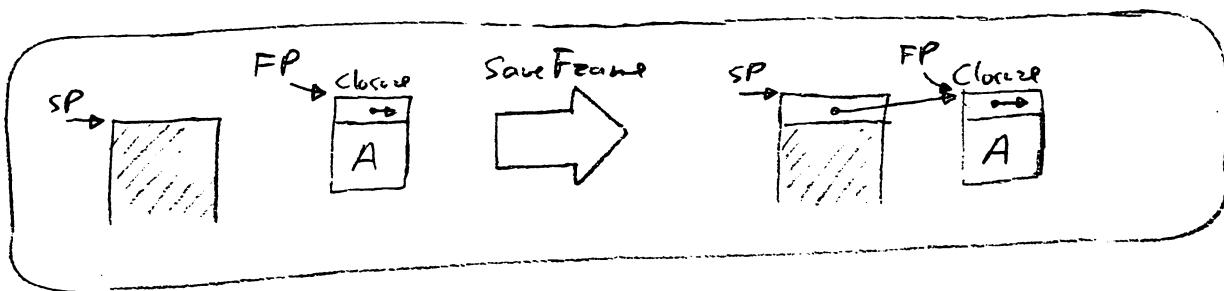
Jump Operations

Jump displacements are expressed in number of skipped instructions - Positive displacements are jumps forward -

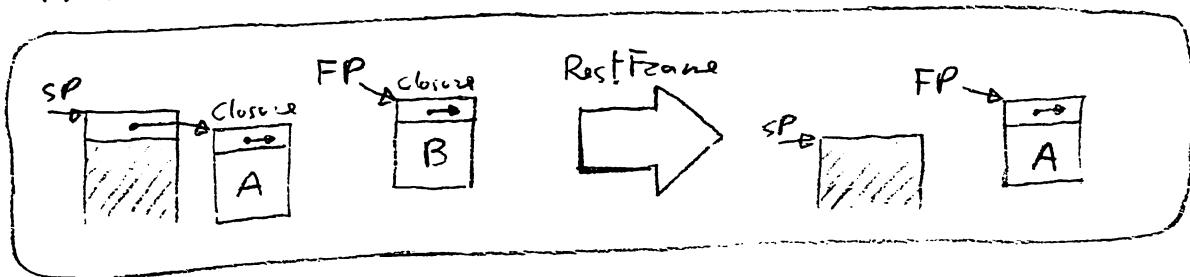
- Jump n (jump leaving AS unchanged)
- TrueJump n (pop AS and jump if the top was "true")
- FalseJump n (pop AS and jump if the top was "false")

Call Operations

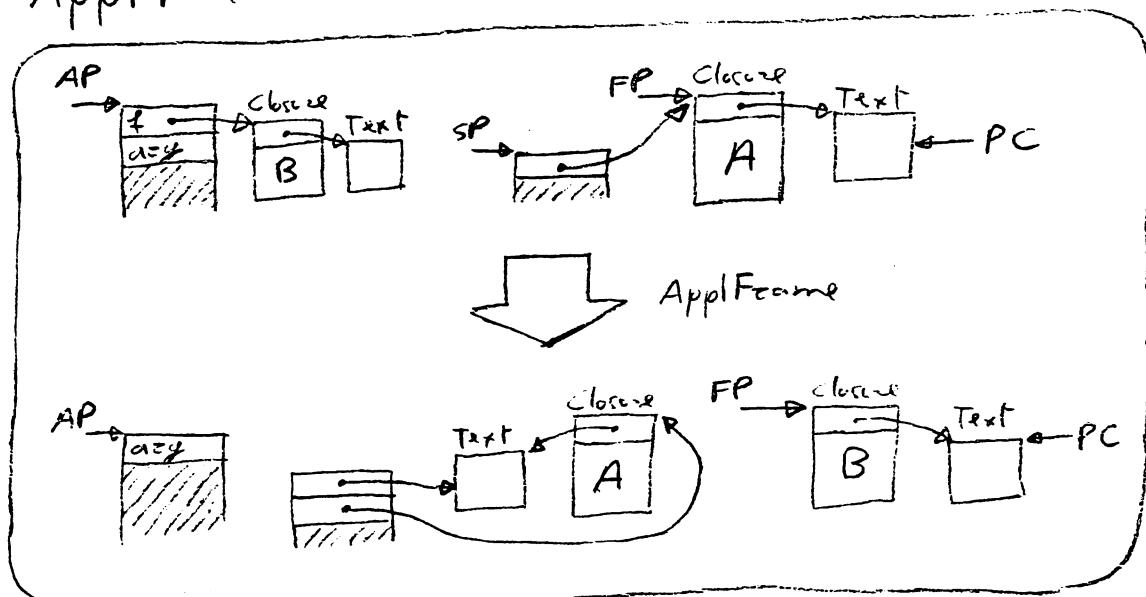
• Save Frame



• Rest Frame

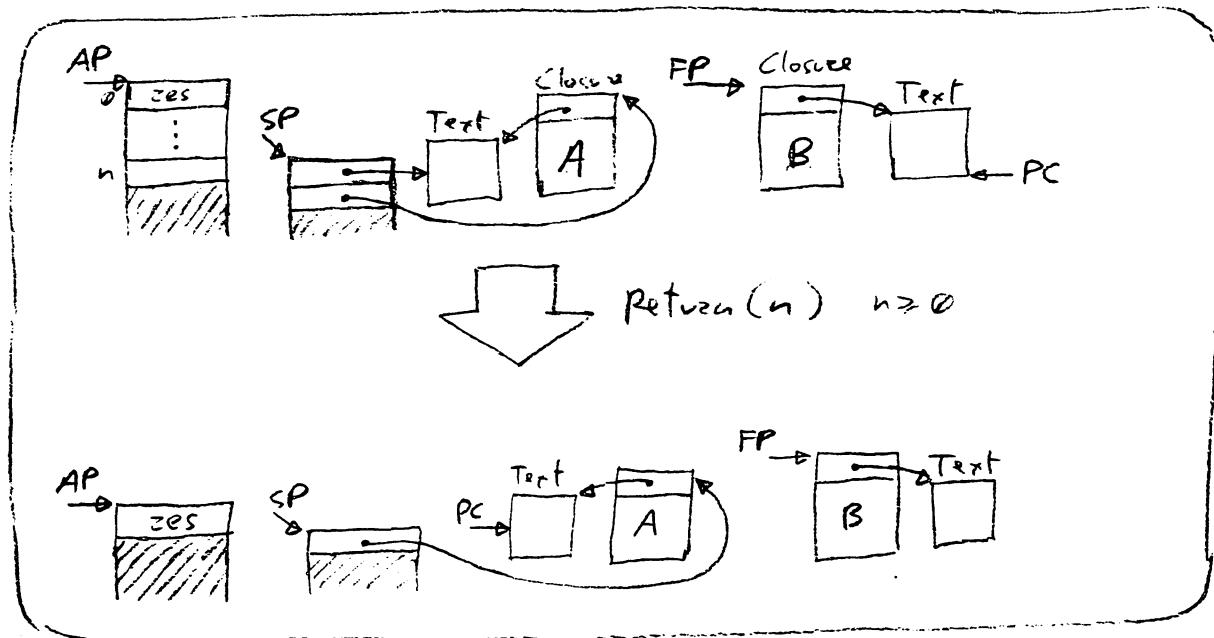


• Appl Frame

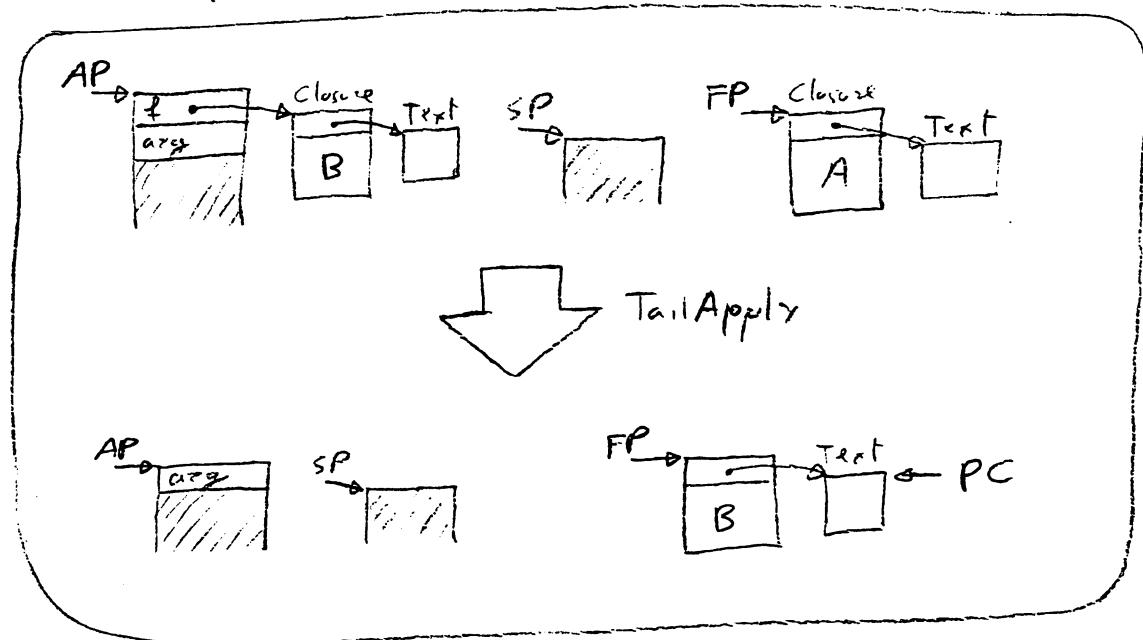


Note: the complete sequence is "SaveFrame; ApplFrame; RestFrame";
A is the callee and B is the called closure

- Return



- Tail Apply

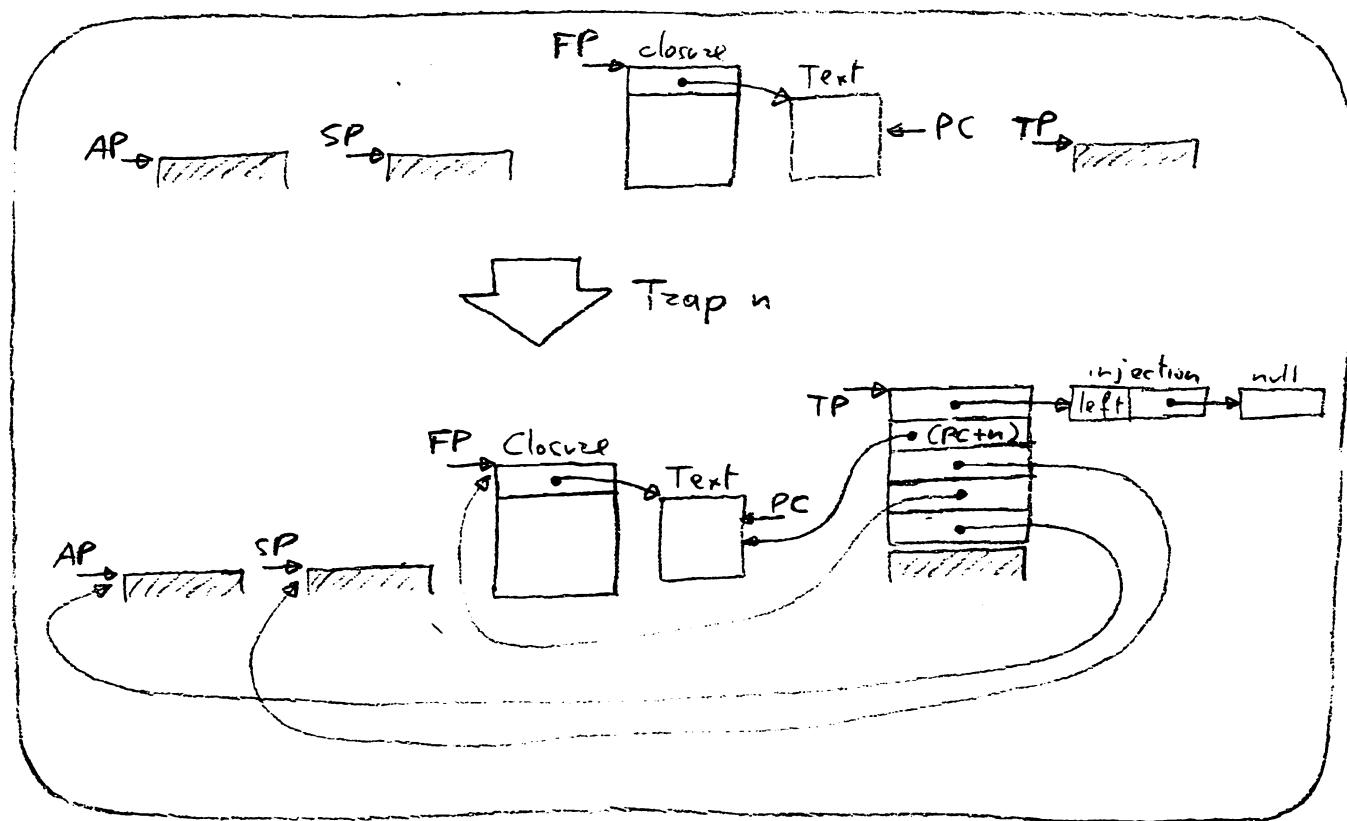


Note: "TailApply" is equivalent to "SaveFrame; ApplFrame; RestFrame; Return"

Fail Operations

A Trap Frame consists of five fields: the first one is a datum of type ".+ trap list" (the trap list) and the other four ones contain PC, SP, FP and AP - Trap jump displacements are expressed in number of skipped instructions. A typical compilation is
"A ? B" → [Trap L1]"A"[UnTrap L2][L1:Pop 1]"B"[L2:]

• Trap

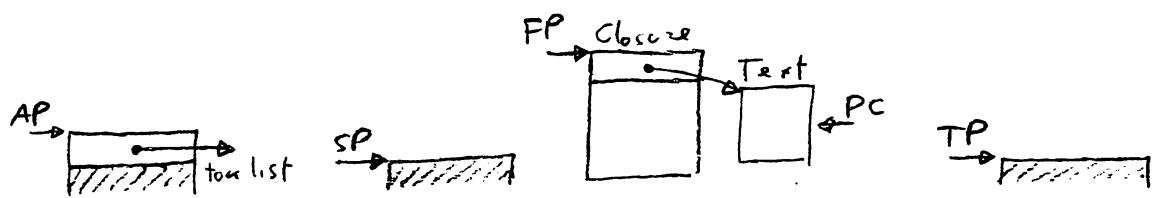


Also:

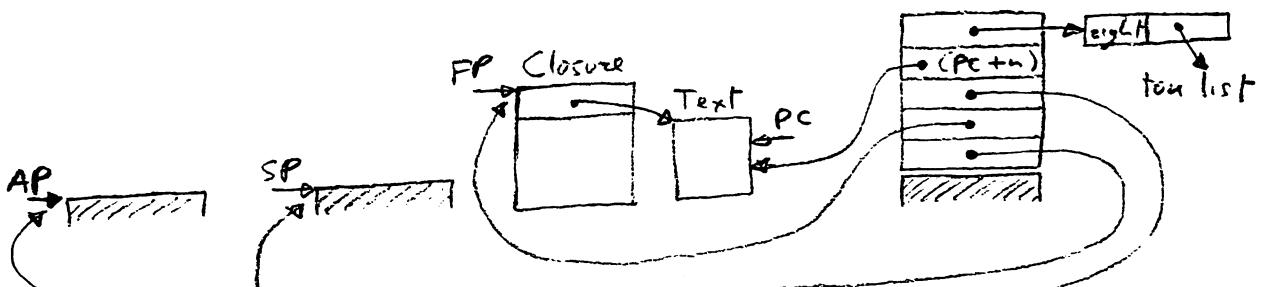
"A ?? ... B" → "... "[TrapList L1]"A"[UnTrap L2][L1:Pop 1]"B"[L2:]

"A ?\x. B" → [Trap L1]"A"[UnTrap L2][L1:]"B"[L2:Squeeze 1]

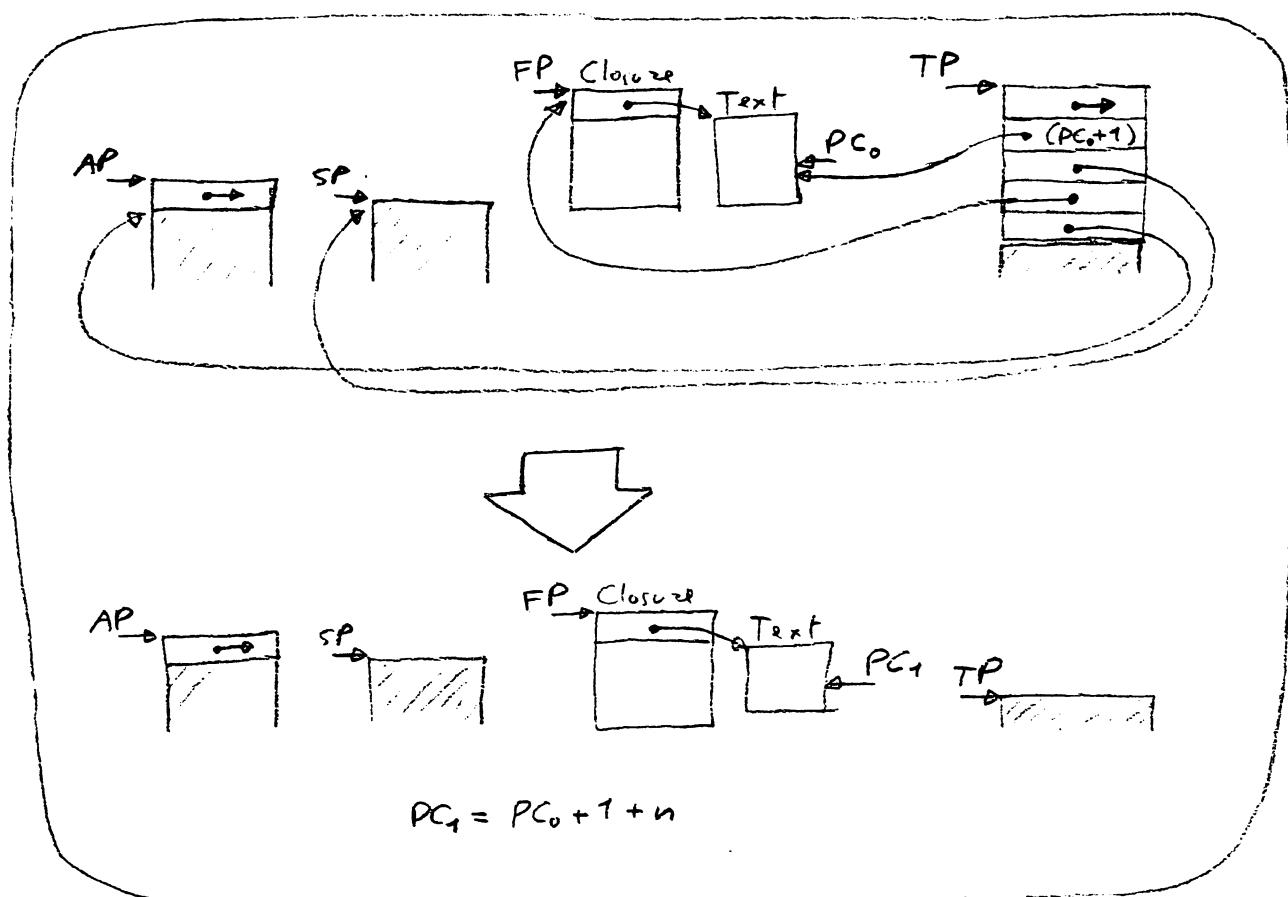
- TrapList



TrapList n

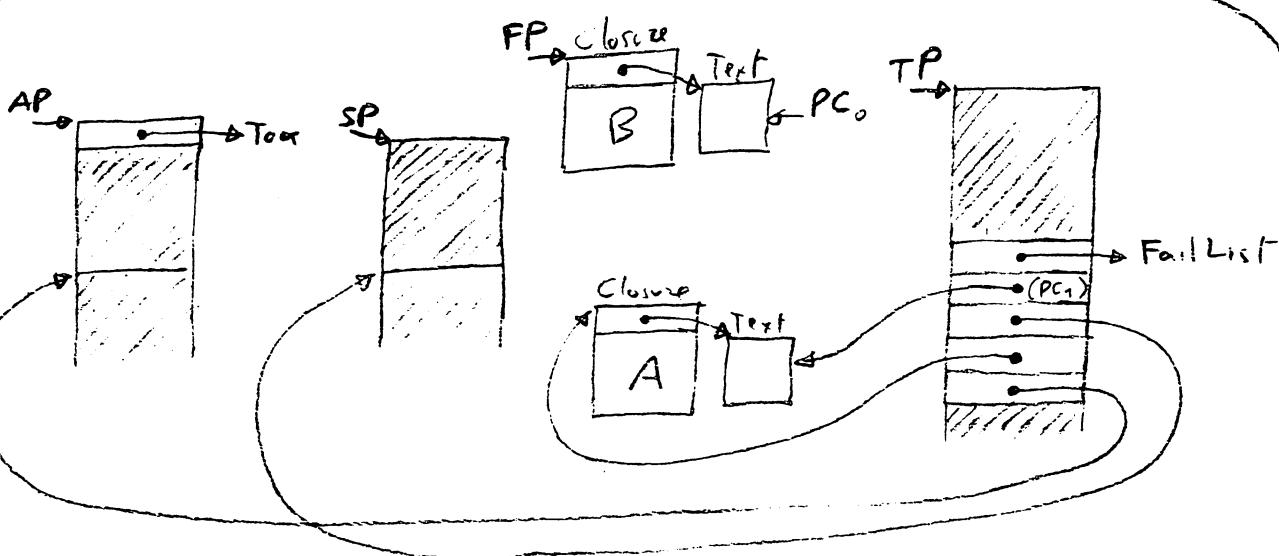


- Untrap

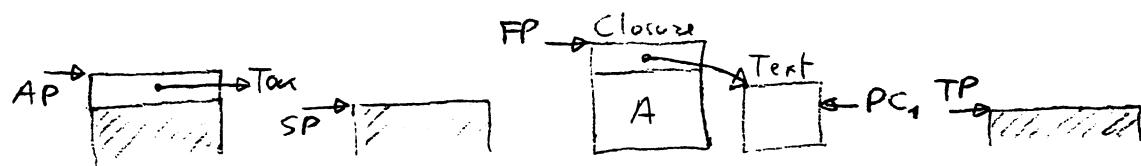


Note: if execution reaches an Untrap, then there have been no (untrapped) failures since the corresponding Trap; hence FP and SP are the same, AP has grown by 1 and PC₀ has almost reached the PC stored in the trap frame (the difference being the Untrap instruction itself). It is then enough to remove the trap frame and skip the failure treatment, jumping to PC₀+1+n -

- FailWith



\downarrow FailWith (*)



(*) If $\text{FailList} = \text{nil}()$ or $\text{FailList} = \text{inc}(\text{TrapList})$ where
 Trap occurs in TrapList -
If no such TrapFrame is found scanning the Trap
Stack from top to bottom, a top-level failure is generated

Note: PC_1 points to the failure recovery text -